

# Bayesian Optimization: From Foundations to Advanced Topics



@deshwal\_aryan



@syrineblk



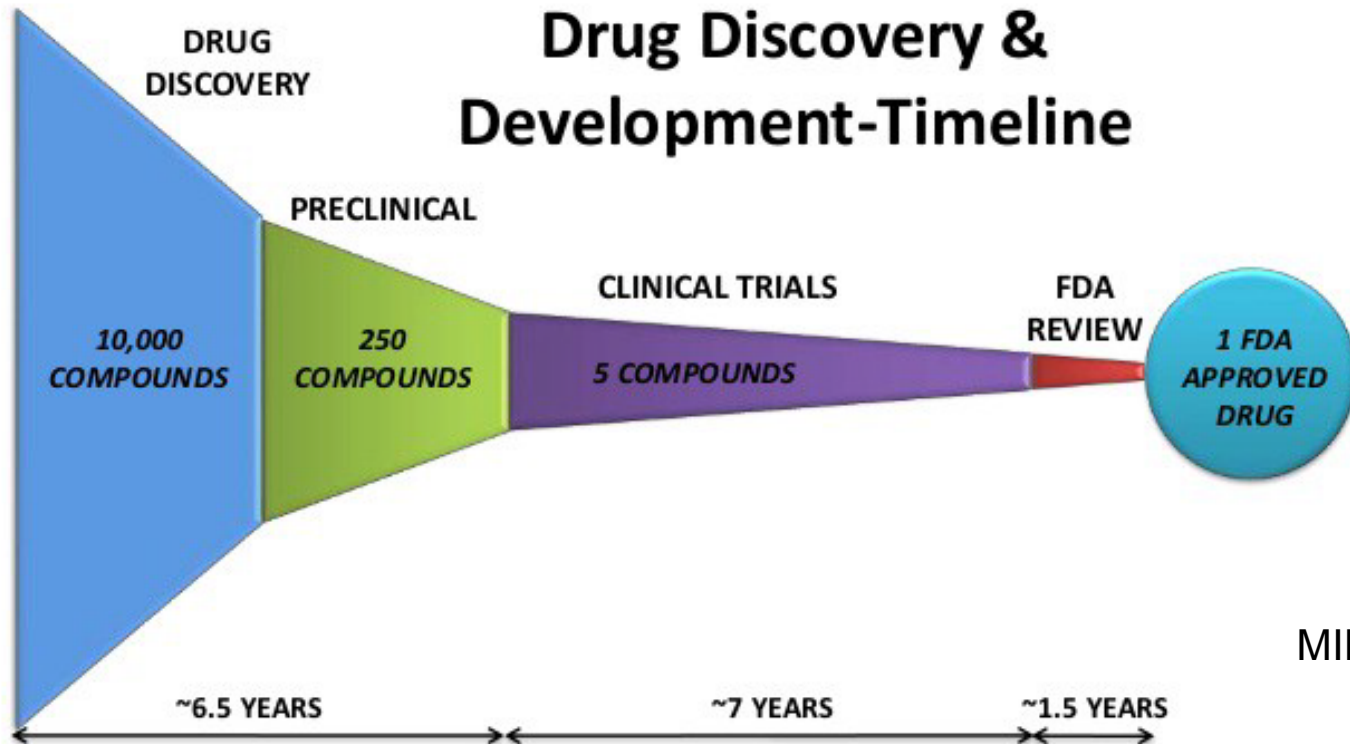
@janadoppa



Half-day Tutorial  
@ AAI-2022 Conference



# Drug/Vaccine Design

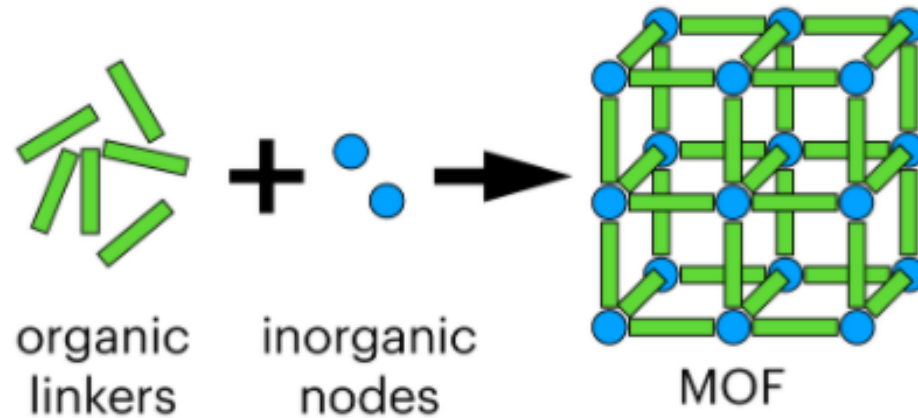


**Credit:**

MIMA healthcare

- Accelerate the discovery of promising designs

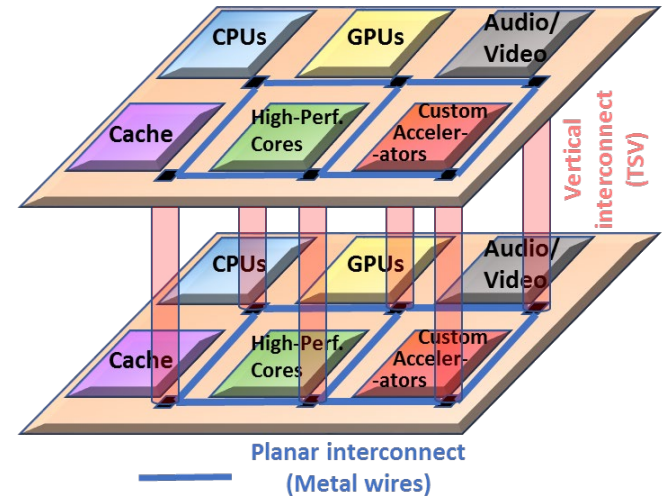
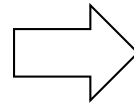
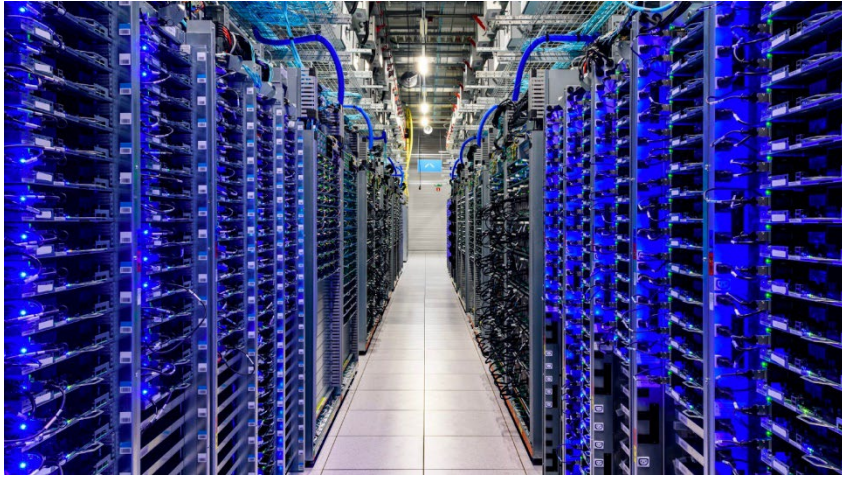
# Nanoporous Materials Design



- **Sustainability applications**

- ▶ Storing gases (e.g., hydrogen powered cars)
- ▶ Separating gases (e.g., carbon dioxide from flue gas of coalfired power plants)
- ▶ Detecting gases (e.g., detecting pollutants in outdoor air)

# Sustainable Hardware Design for Data Centers



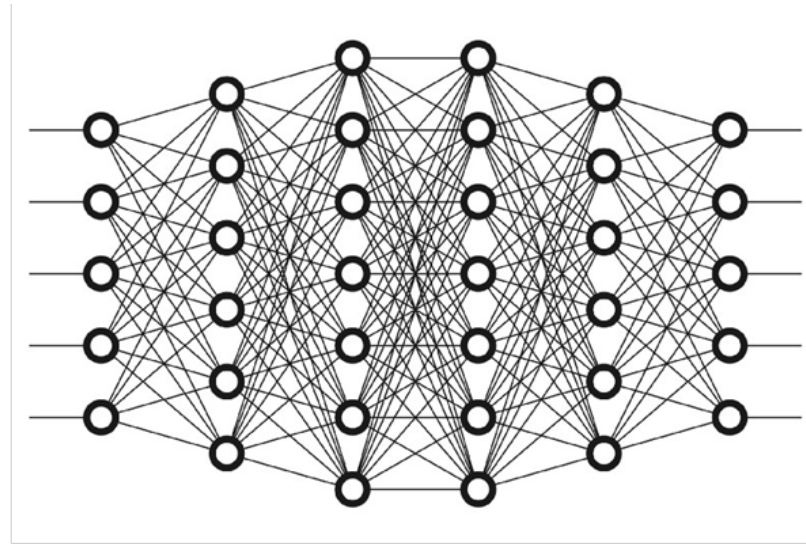
## America's Data Centers Are Wasting Huge Amounts of Energy

By 2020, data centers are projected to consume roughly 140 billion kilowatt-hours annually, costing American businesses \$13 billion annually in electricity bills and emitting nearly 150 million metric tons of carbon pollution

## High-performance and Energy-efficient manycore chips

Report from Natural Resources Defense Council:  
<https://www.nrdc.org/sites/default/files/data-center-efficiency-assessment-IB.pdf>

# Auto ML and Hyperparameter Tuning

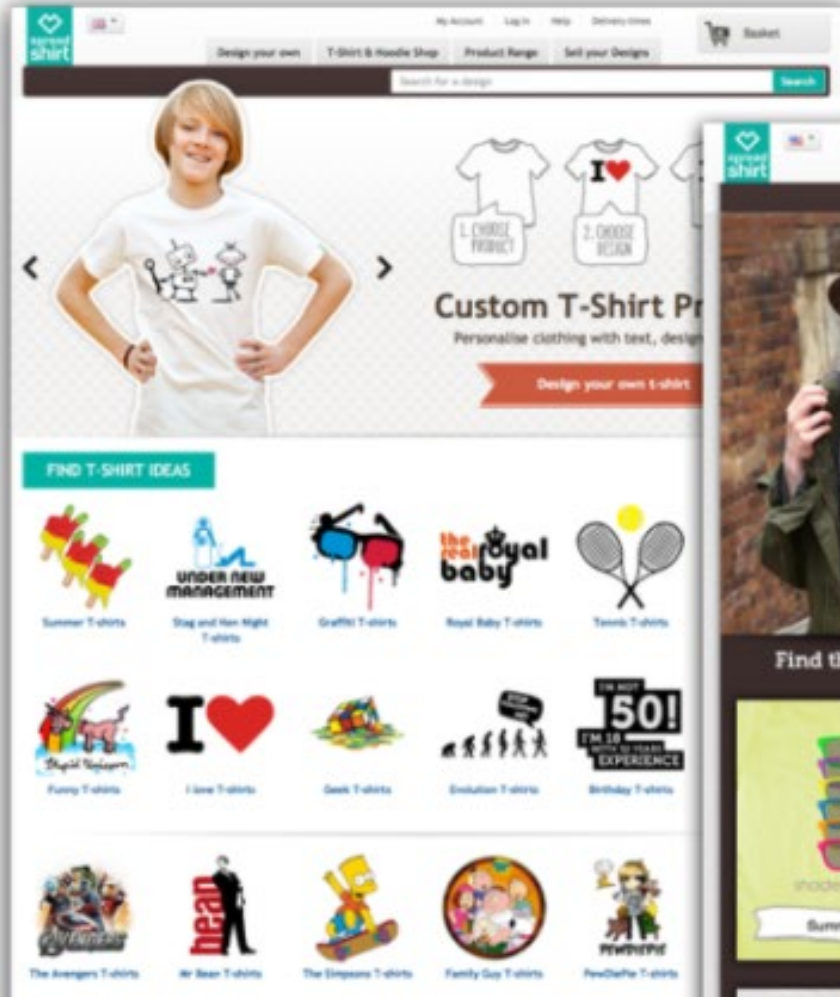


- Accuracy of models critically depends on hyper-parameters
  - ▲ Optimization algorithm, learning rates, momentum, batch normalization, batch sizes, dropout rates, weight decay, data augmentation, ...

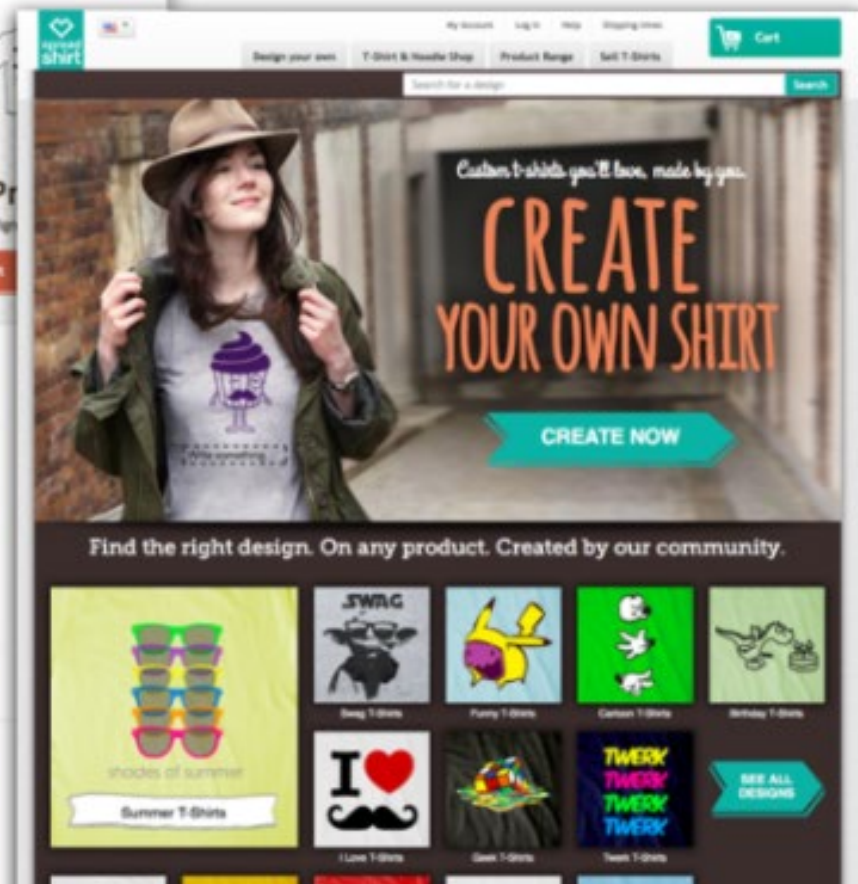


# A/B Testing to Configure Websites

## Original



## Variation



# Making Delicious Cookies



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## Bayesian Optimization for a Better Dessert

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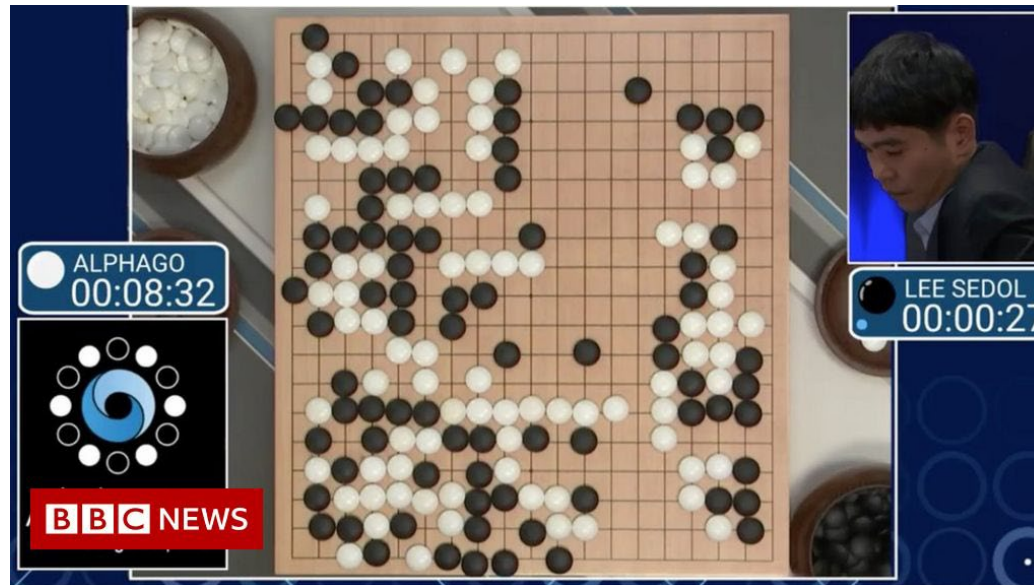
**Greg Kochanski, Daniel Golovin, John Karro, Benjamin Solnik,  
Subhdeep Moitra, and D. Sculley**

{gpk, dgg, karro, bsolnik, smoitra, dsculley}@google.com; Google Brain Team

### Abstract

We present a case study on applying Bayesian Optimization to a complex real-world system; our challenge was to optimize chocolate chip cookies. The process was a mixed-initiative system where both human chefs, human raters, and a machine optimizer participated in 144 experiments. This process resulted in highly rated cookies that deviated from expectations in some surprising ways – much less sugar in California, and cayenne in Pittsburgh. Our experience highlights the importance of incorporating domain expertise and the value of transfer learning approaches.

# Making AlphaGo Better



## Bayesian Optimization in AlphaGo

Yutian Chen, Aja Huang, Ziyu Wang, Ioannis Antonoglou, Julian Schrittwieser,  
David Silver & Nando de Freitas

DeepMind, London, UK  
yutianc@google.com

### Abstract

During the development of AlphaGo, its many hyper-parameters were tuned with Bayesian optimization multiple times. This automatic tuning process resulted in substantial improvements in playing strength. For example, prior to the match with Lee Sedol, we tuned the latest AlphaGo agent and this improved its win-rate from 50% to 66.5% in self-play games. This tuned version was deployed in the final match. Of course, since we tuned AlphaGo many times during its development cycle, the compounded contribution was even higher than this percentage. It is our hope that this brief case study will be of interest to Go fans, and also provide Bayesian optimization practitioners with some insights and inspiration.

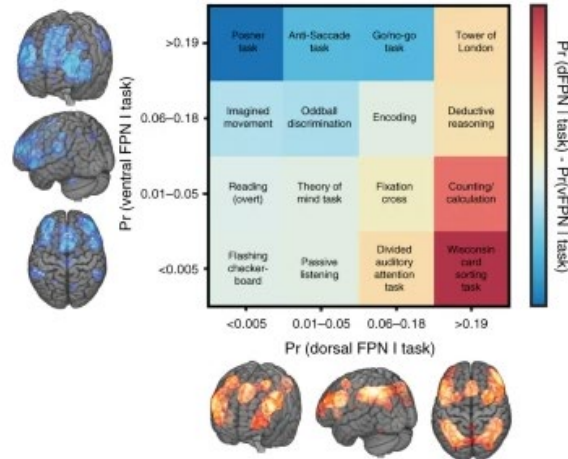


# Neuroscience and Brain Analytics

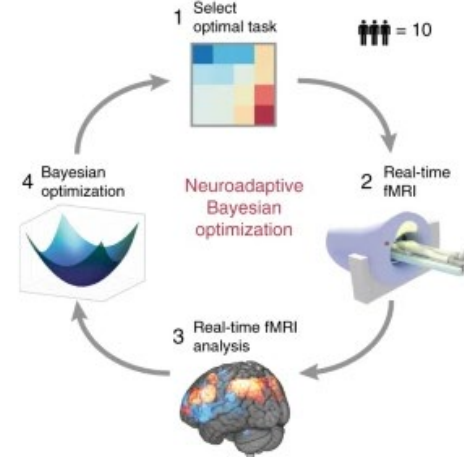
**a**

## Experiment 1

Task space based on meta-analysis



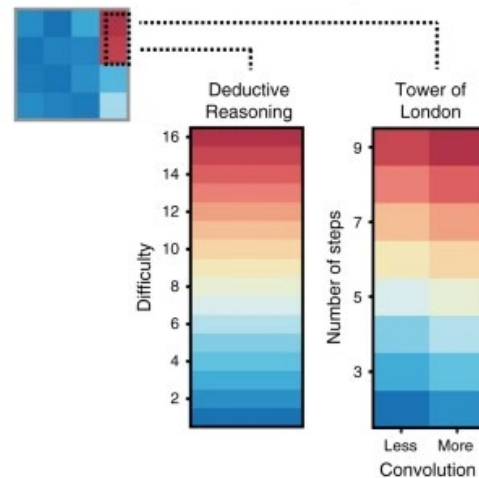
Real-time experiment: selecting tasks



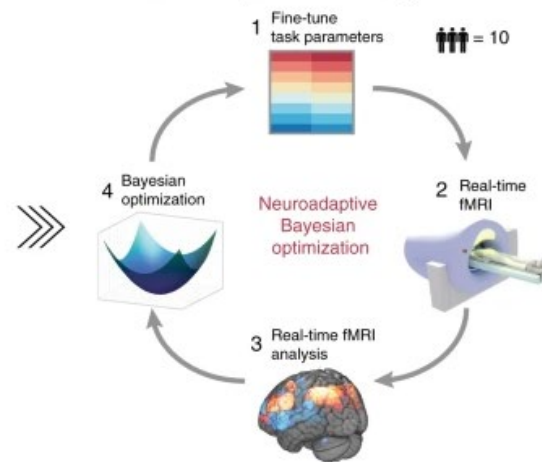
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## Experiment 2

Modifiable variants of tasks selected in Experiment 1



Real-time experiment: fine-tuning tasks

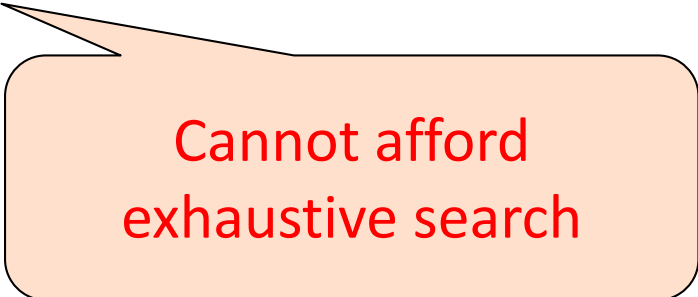


# Common Attributes of the Search Problem

- **Search Space:** Many candidate choices (inputs)
- **Objective function:** Need to perform an expensive experiment to evaluate the objective value of any input
- **Optimization problem:** find the candidate input with highest objective function value

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Cannot afford  
exhaustive search

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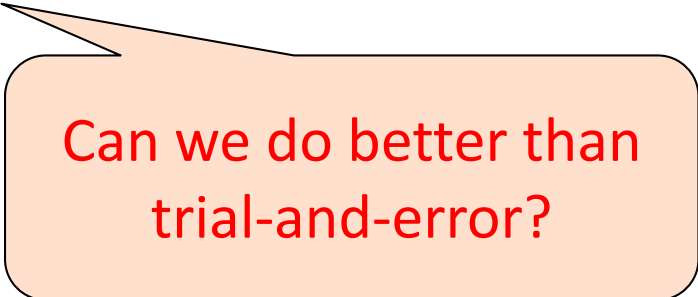
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Trial and Error?

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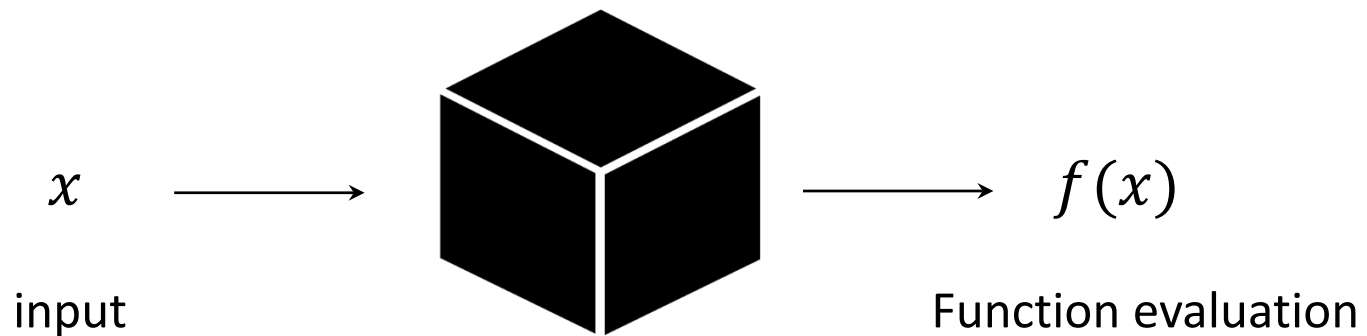
Can we do better than trial-and-error?



# Accelerate Search via Bayesian Optimization

- Efficiently optimize **expensive** black-box functions

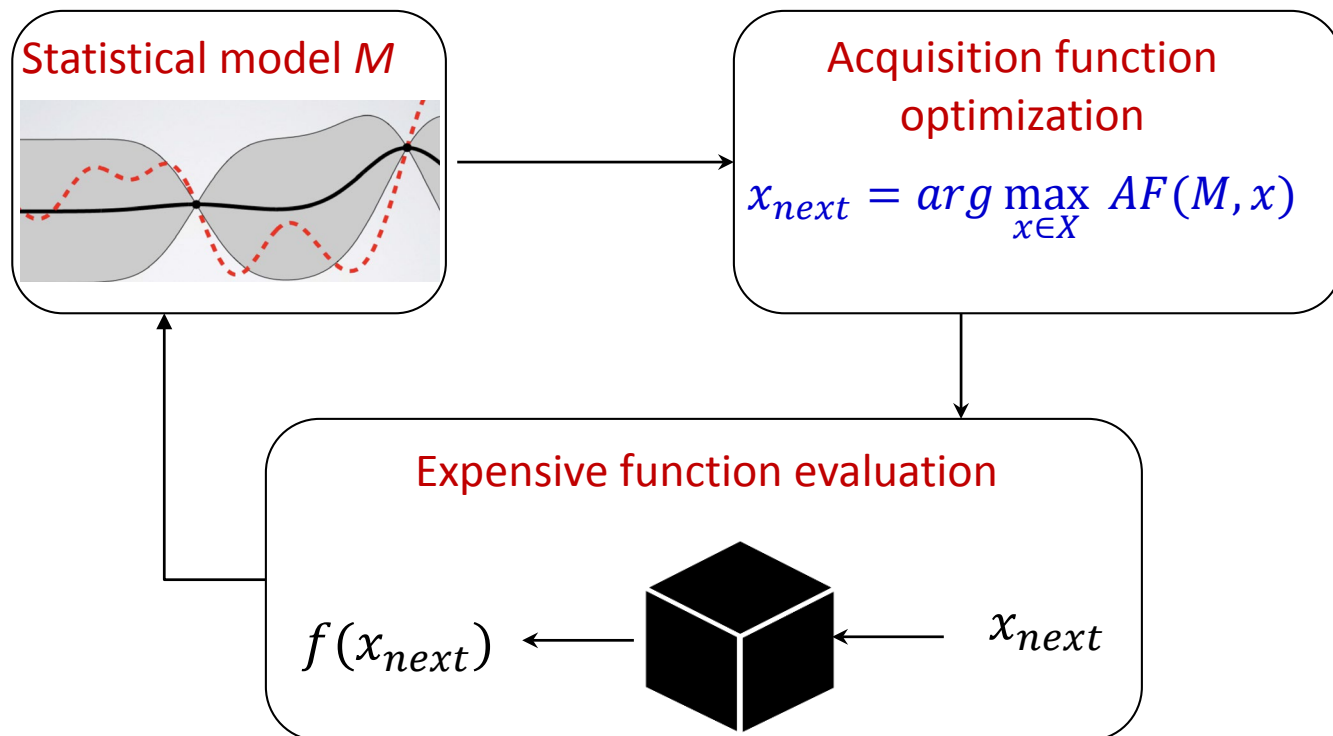
$$x^* = \mathop{\text{arg max}}_{x \in X} f(x)$$



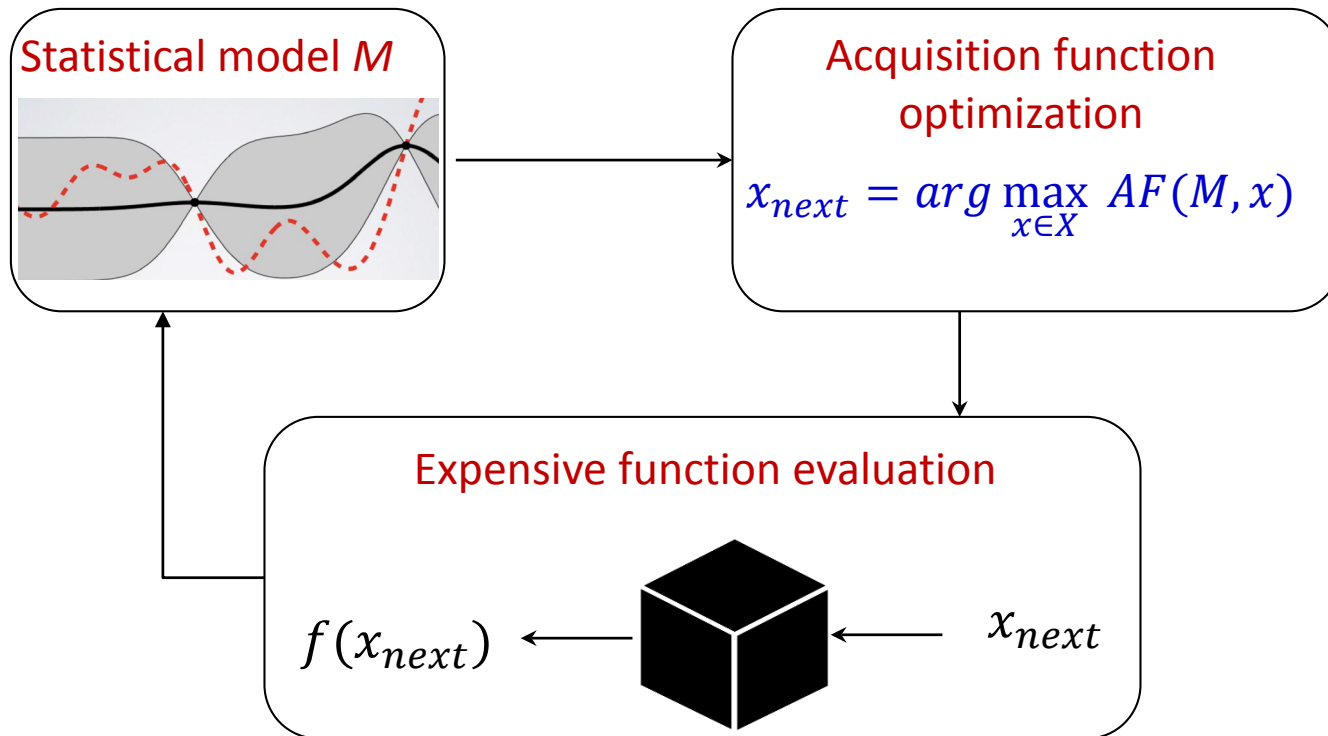
- Black-box queries (aka experiments) are **expensive**

# Bayesian Optimization: Key Idea

- Build a **surrogate statistical model** and use it to intelligently search the space
  - ▲ Replace expensive queries with **cheaper queries**
  - ▲ Use **uncertainty** of the model to select expensive queries



# Bayesian Optimization: Three Key Elements



- Statistical model (e.g., Gaussian process)
- Acquisition function (e.g., Expected improvement)
- Acquisition function optimizer (e.g., local search)

# BO Dimensions: Input Space

- **Continuous space**
  - ▲ All variables of input  $x$  are continuous
- **Discrete / Combinatorial space**
  - ▲ Sequences, trees, graphs, sets, permutations etc.
- **Hybrid space**
  - ▲  $x$  = mixture of  $x_d$  (discrete) and  $x_c$  (continuous) variables

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Most of the focus of  
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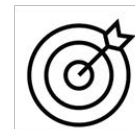
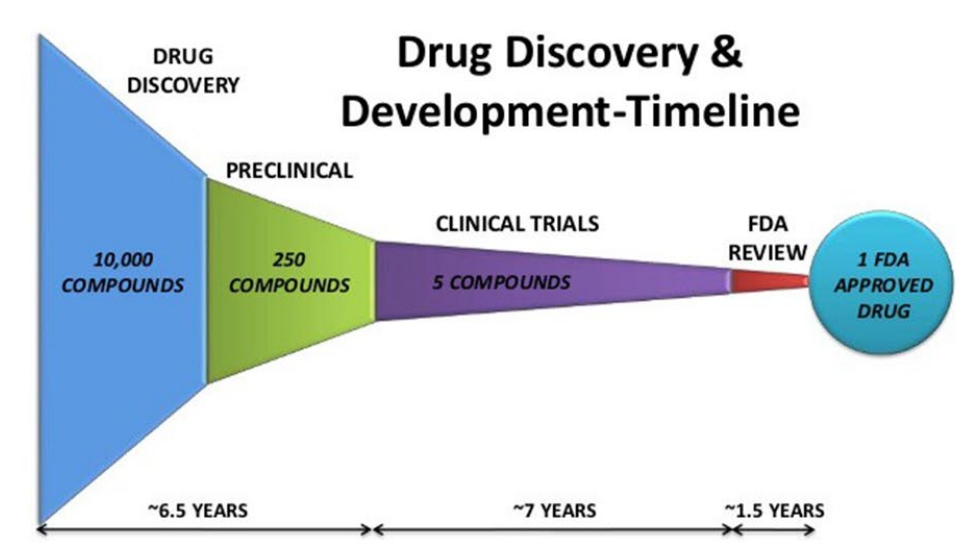


# BO Dimensions: No. of Objectives

- **Single objective**

- ▲ For example, finding hyperparameters to optimize accuracy

- **Multiple objectives**



Effectiveness



Safety



Cost



# BO Dimensions: No. of Objectives

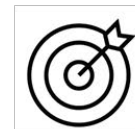
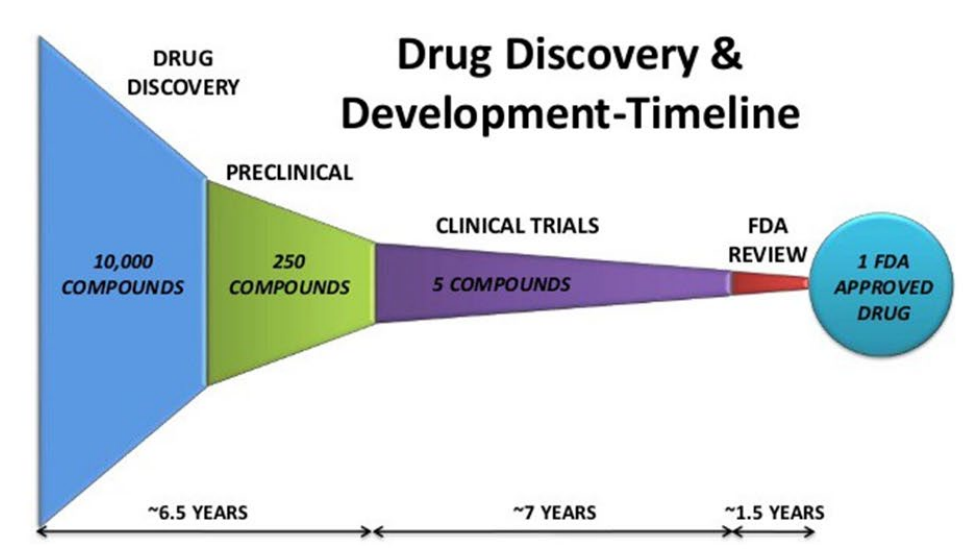
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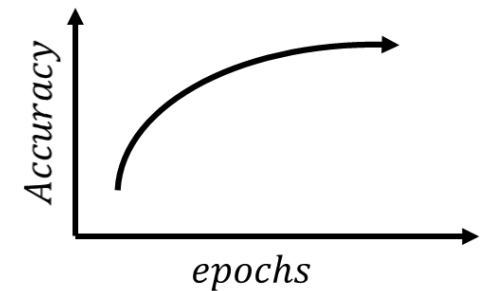
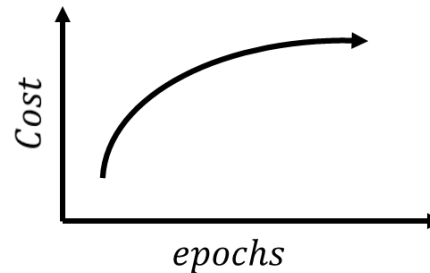
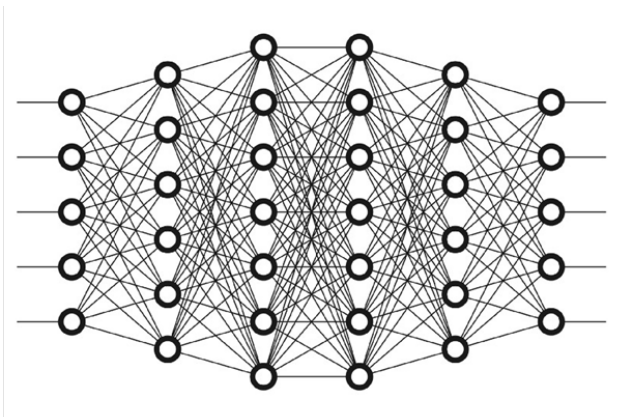
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- **Single-fidelity setting**

- ▶ Most expensive and accurate function evaluation

- **Multi-fidelity setting**

- ▶ Function evaluations with varying trade-offs in cost and accuracy



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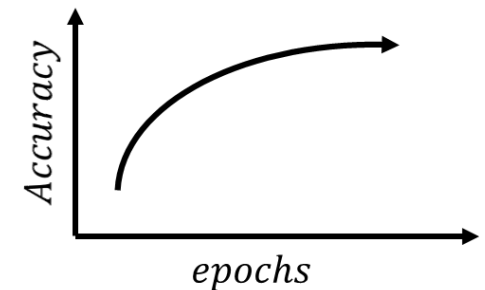
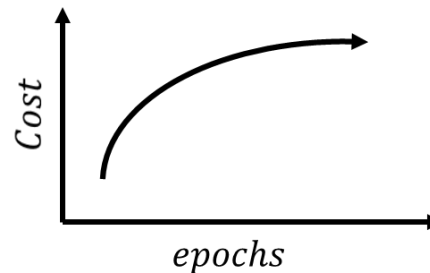
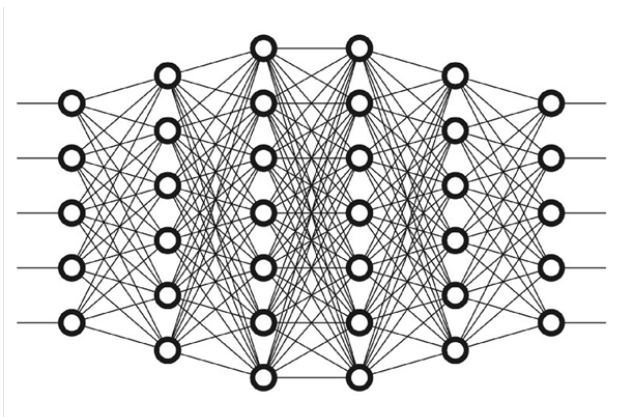
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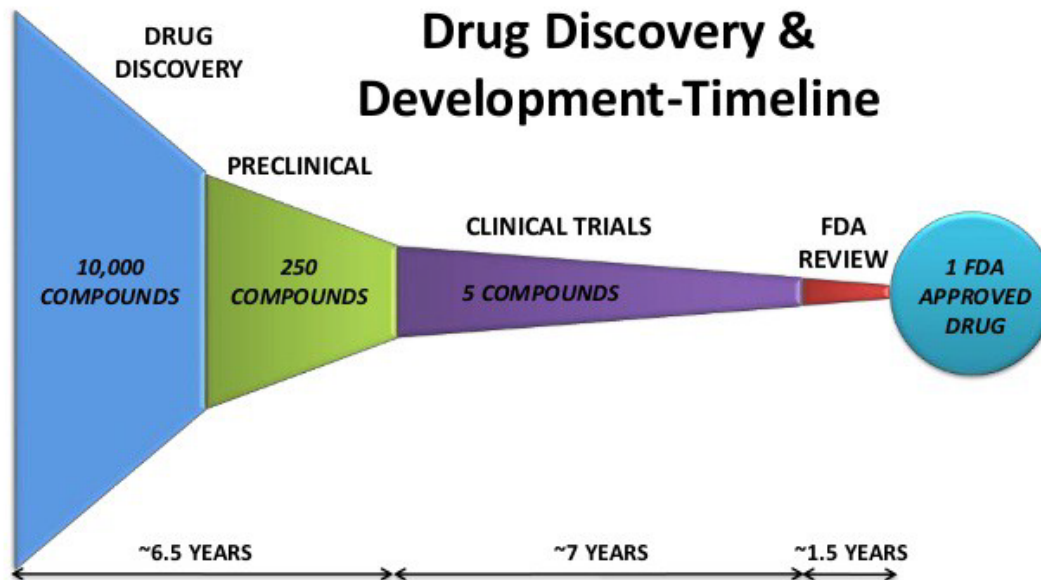


# BO Dimensions: Constraints

- **Unconstrained setting**

- ▲ all inputs are valid

- **Constrained setting**



Drugs/Vaccines  
that are safe



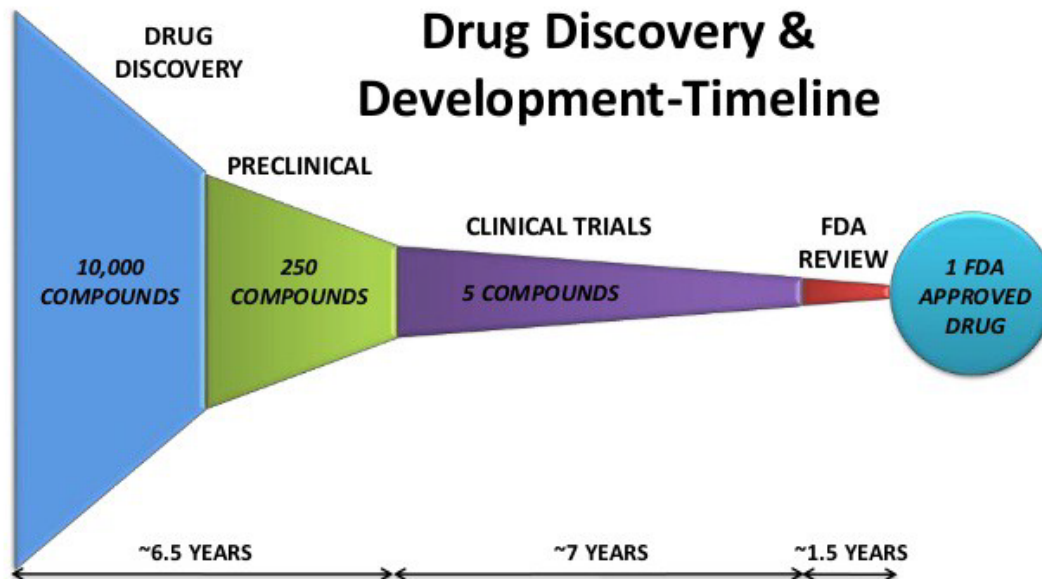
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Drugs/Vaccines that are safe

# Outline of the Tutorial

- Background on GPs and Single-Objective BO
- Bayesian Optimization over Combinatorial Spaces
- Bayesian Optimization over Hybrid Spaces

## Break

- Multi-Fidelity Bayesian Optimization
- Constrained Bayesian Optimization
- Multi-Objective Bayesian Optimization
- Summary and Outstanding Challenges in BO